

Pattern formation and criticality during social contagions

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SYDNEY

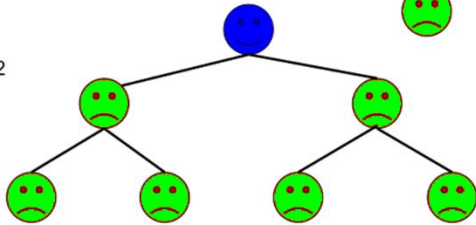
CCS Workshop on
“Evolution of Social Complexity”
21 February 2024

- Types of social contagions
- Maximum Entropy Principle and bounded rationality
- Pattern formation during social dynamics
- Tipping points during the COVID-19 pandemic

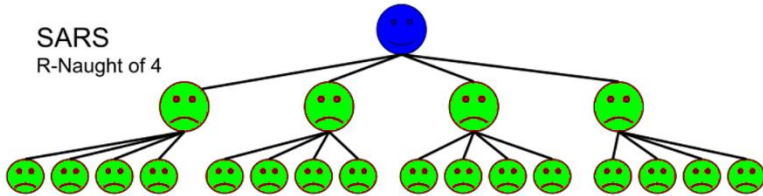
 Patient Zero

 Infected

Ebola:
R-Naught of 2



SARS
R-Naught of 4

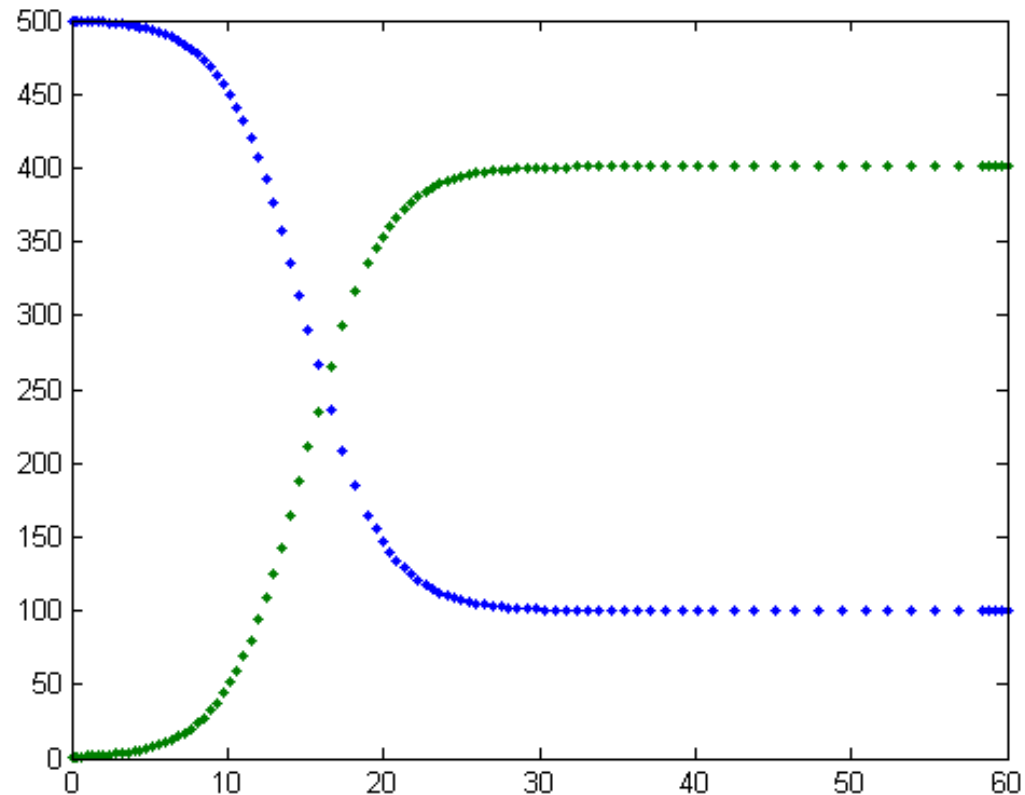


$$\frac{dS}{dt} = \gamma I - \beta IS$$

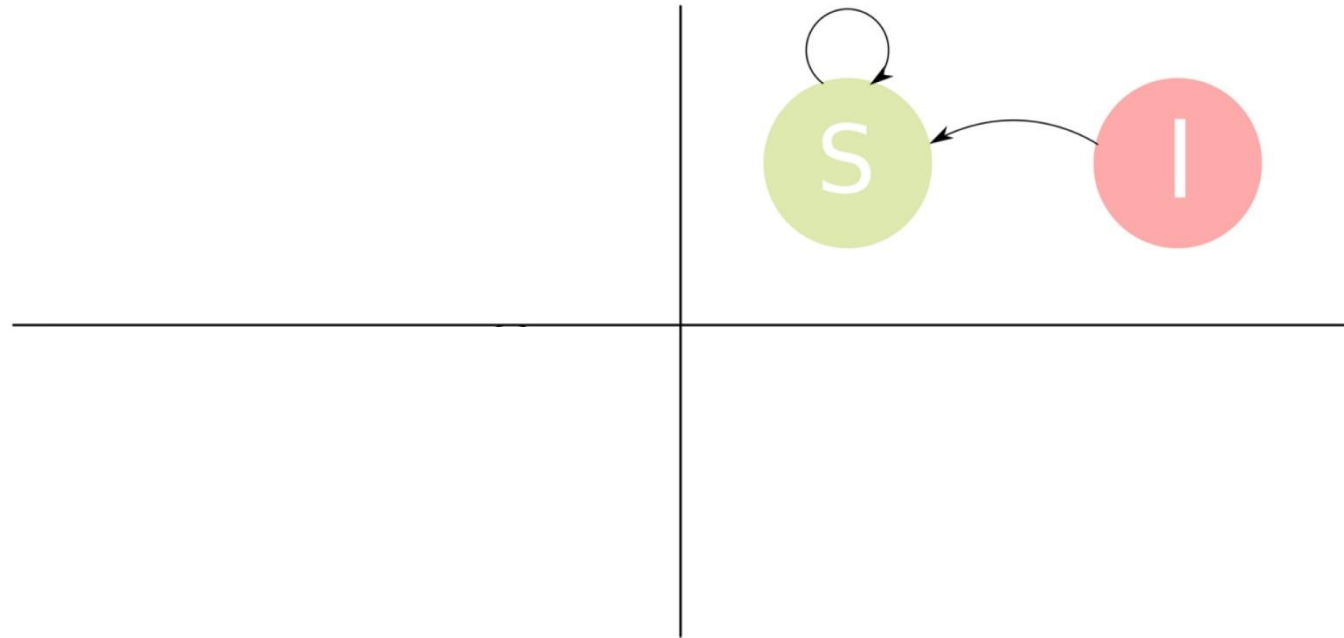
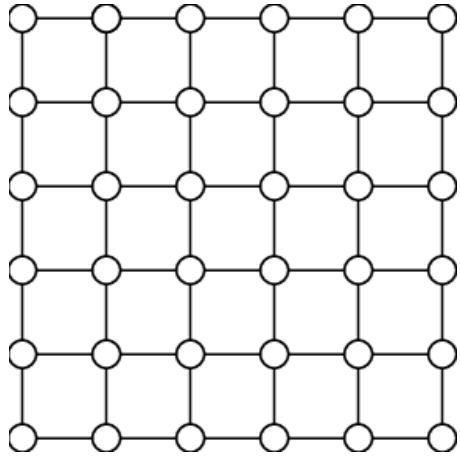
$$\frac{dI}{dt} = \beta IS - \gamma I,$$

$$\beta / \gamma = R_0$$

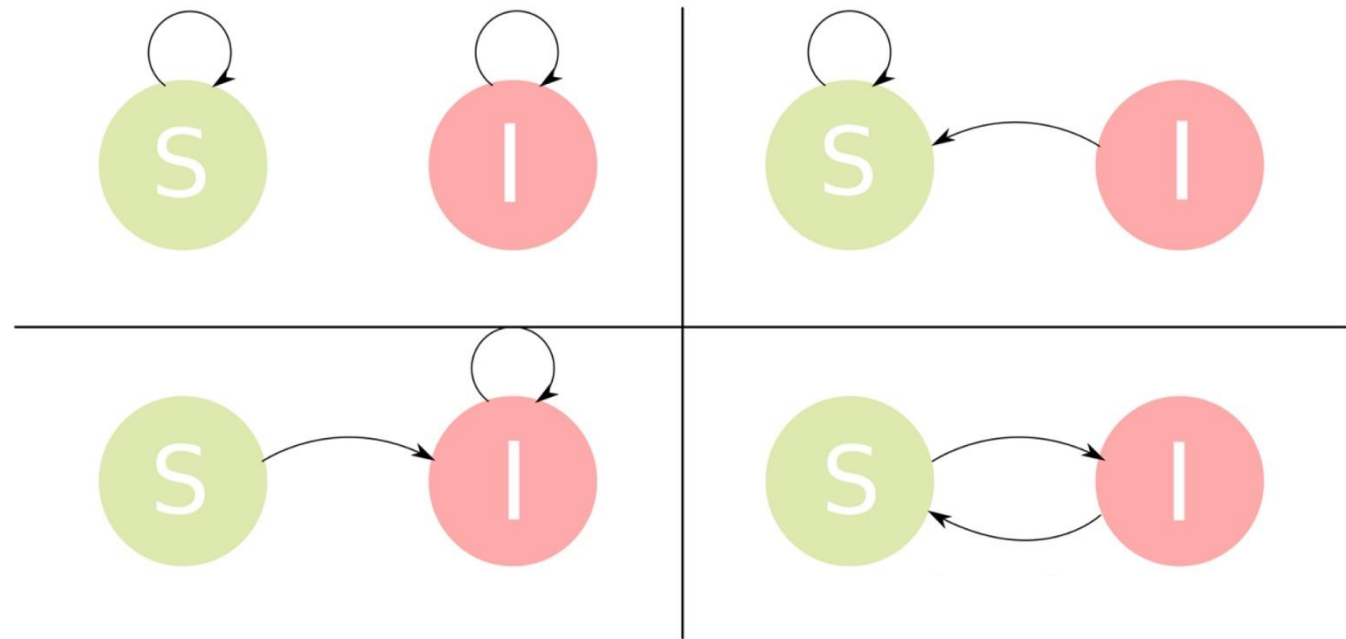
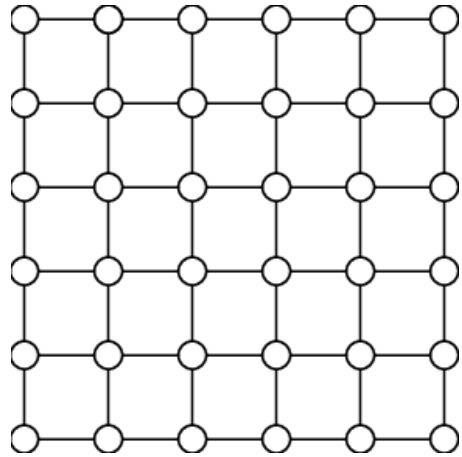
SIS: Susceptible - Infectious - Susceptible



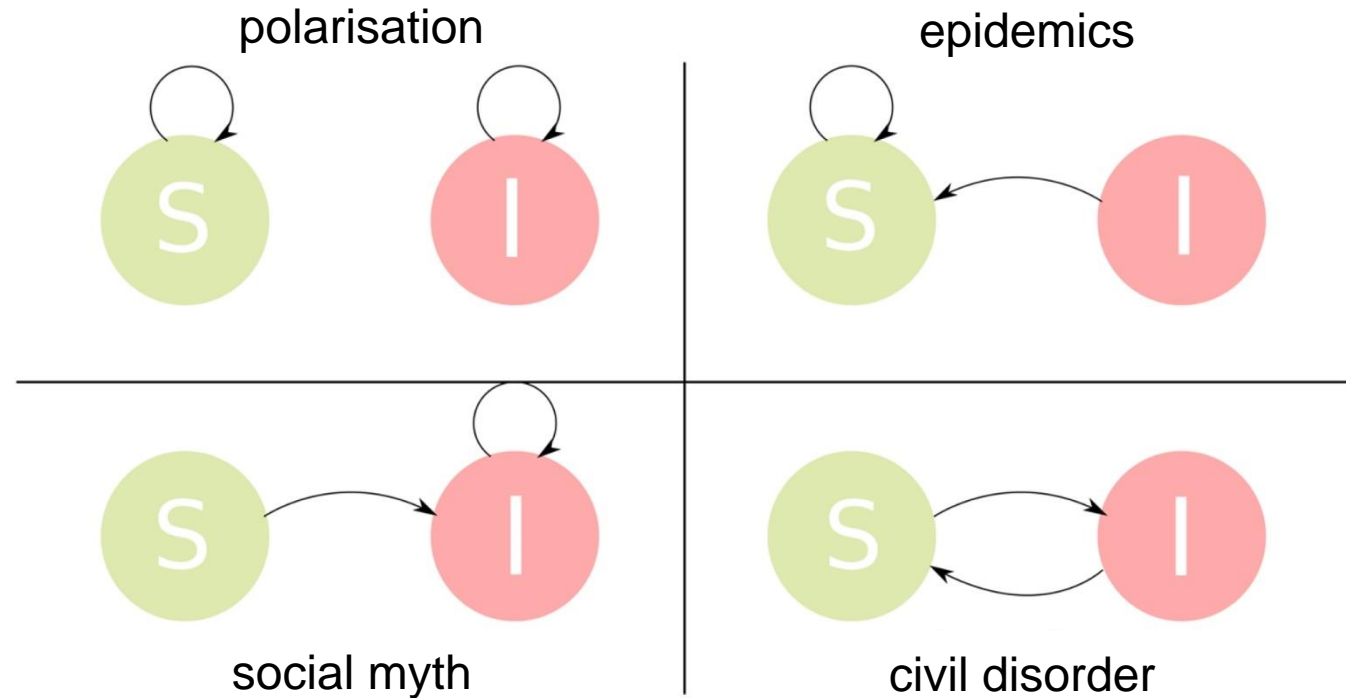
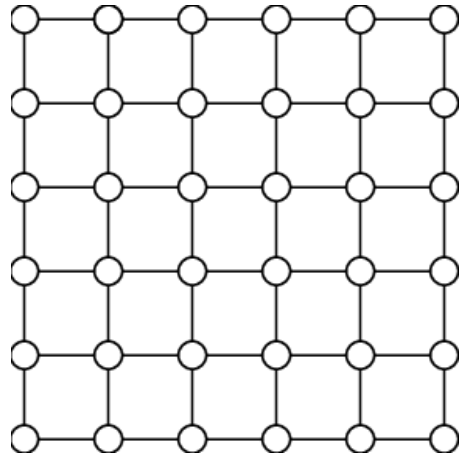
Social contagions: four types of dynamics



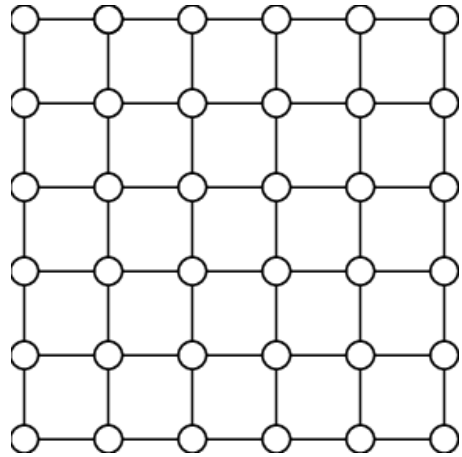
Social contagions: four types of dynamics



Social contagions: four types of dynamics




Dynamic meta-population epidemic (SIS) model



$$\frac{dI_i}{dt} = -\gamma I_i + \beta \sum_{j,k} \phi_{ij}^S(\mathbf{I}, \mathbf{C}) \phi_{kj}^I(\mathbf{I}, \mathbf{C}) \frac{S_i I_k}{\hat{N}_j(\mathbf{I}, \mathbf{C})}$$

$$\hat{N}_j(\mathbf{I}, \mathbf{C}) = \sum_k S_k \phi_{kj}^S(\mathbf{I}, \mathbf{C}) + I_k \phi_{kj}^I(\mathbf{I}, \mathbf{C})$$

Benefit



$$b_j = N_j^{-1}(N_j - I_j)$$

Boltzmann-Lotka-Volterra spatial interaction

MaxEnt
Principle

$$H_Y = - \sum_y p_Y(y) \ln p_Y(y)$$

constraints

$$B^I = \sum_{i,j} I_i \phi_{ij}^I(\mathbf{I}, \mathbf{C}) b_j / \sum_i I_i,$$

vs

control
parameters

$$B^S = \sum_{i,j} S_i \phi_{ij}^S(\mathbf{I}, \mathbf{C}) b_j / \sum_i S_i$$

$$C = \sum_{i,j} (I_i \phi_{ij}^I(\mathbf{I}, \mathbf{C}) + S_i \phi_{ij}^S(\mathbf{I}, \mathbf{C})) c_{ij} / \sum_i (I_i + S_i)$$

Boltzmann-Lotka-Volterra spatial interaction

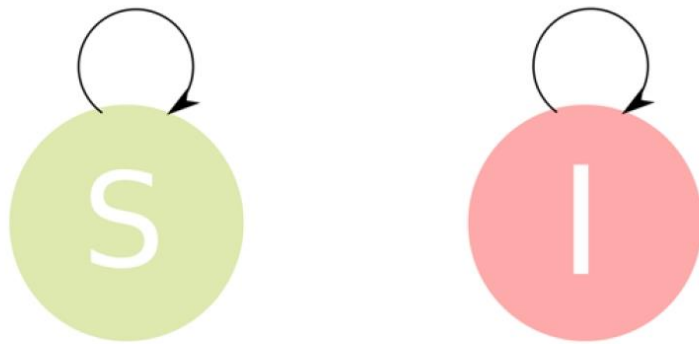
MaxEnt
Principle

$$H_Y = - \sum_y p_Y(y) \ln p_Y(y)$$

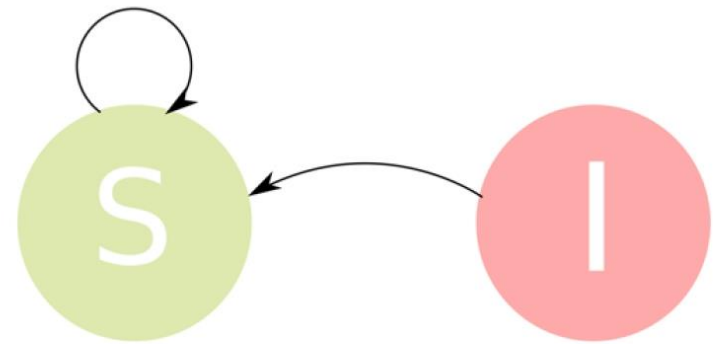
$$\begin{pmatrix} \alpha^S \\ \alpha^I \\ \omega \end{pmatrix} \begin{array}{l} \text{Specify constraints: Infer model parameters} \\ \iff \\ \text{Specify parameters: Model generates quantities} \end{array} \begin{pmatrix} B^S \\ B^I \\ C \end{pmatrix}$$

Bounded rationality: four types of dynamics

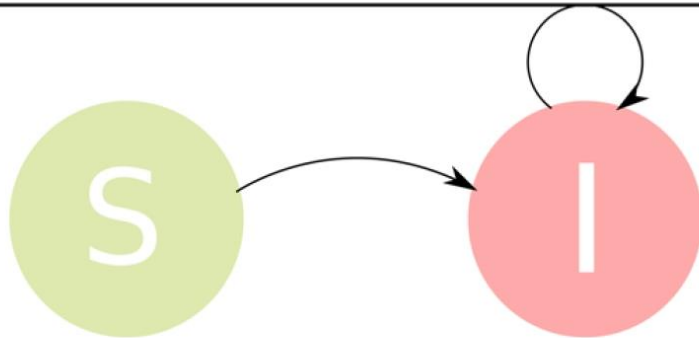
$$\phi_{ij}^x(\mathbf{I}, \mathbf{C} | \alpha^x, \omega) = Z_{x,i}^{-1} \exp(\alpha^x b_j - \omega c_{ij})$$



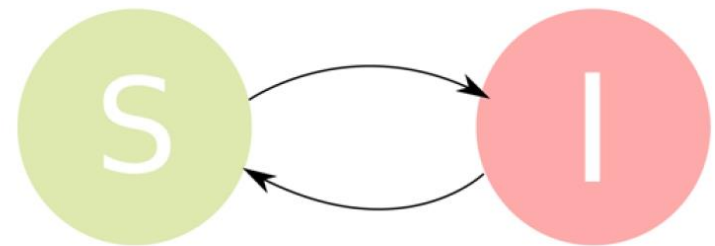
$$\alpha^I < 0, \alpha^S > 0$$



$$\alpha^I > 0, \alpha^S > 0$$



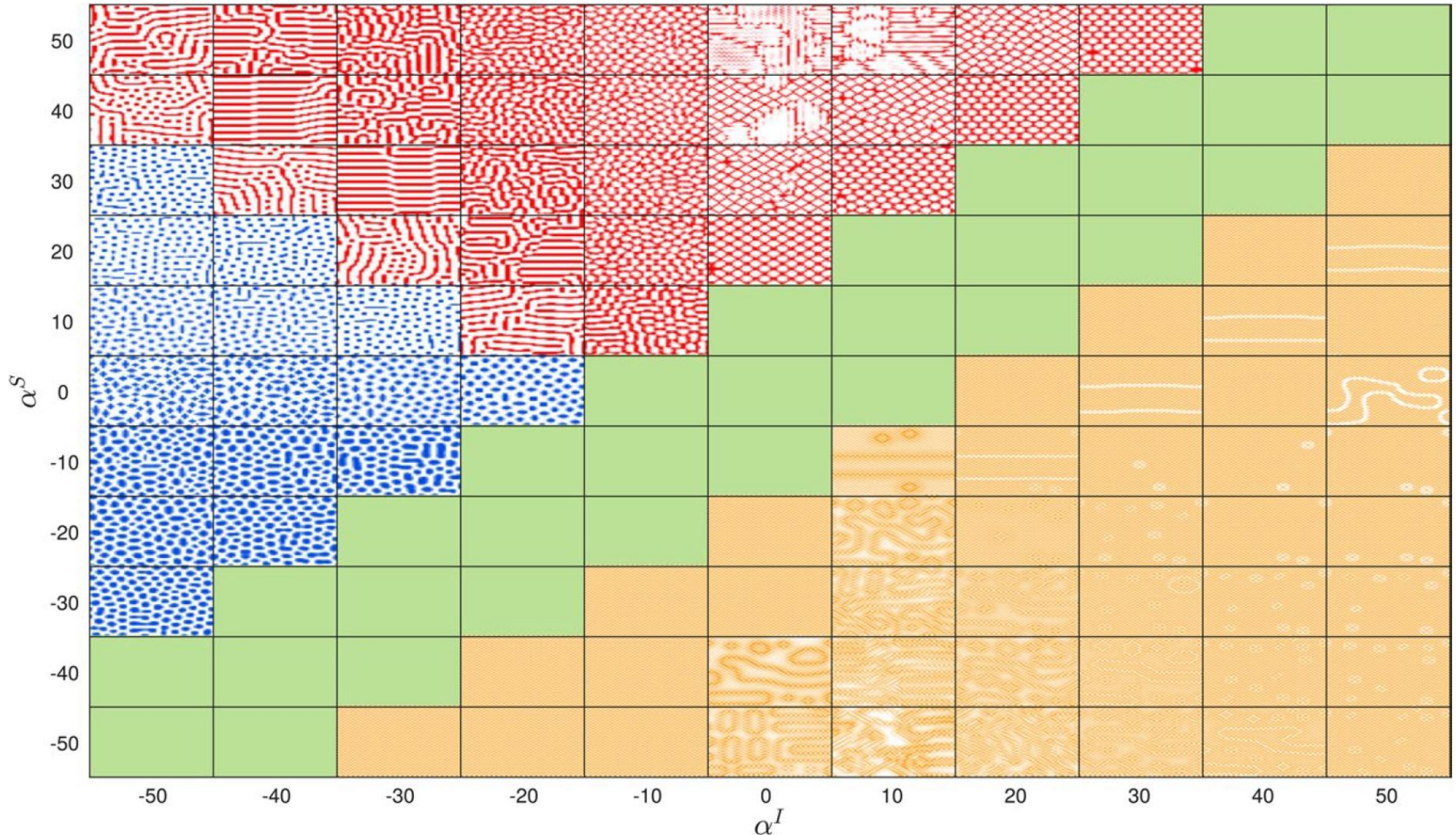
$$\alpha^I < 0, \alpha^S < 0$$



$$\alpha^I > 0, \alpha^S < 0$$

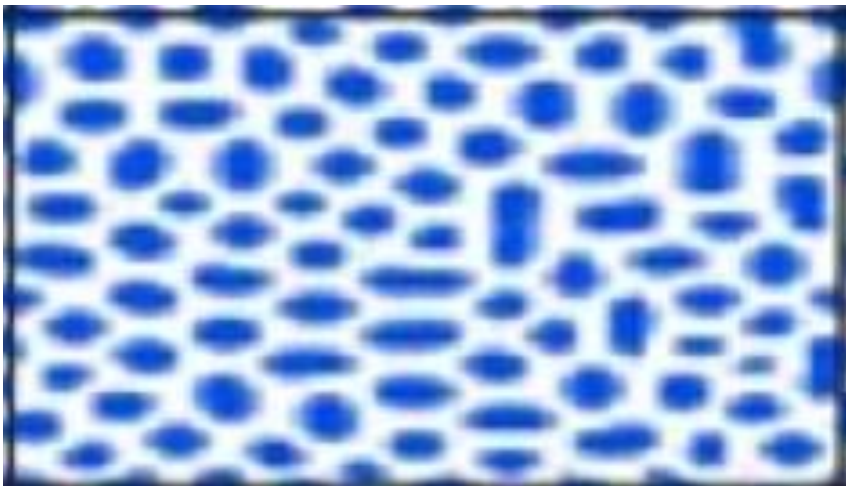
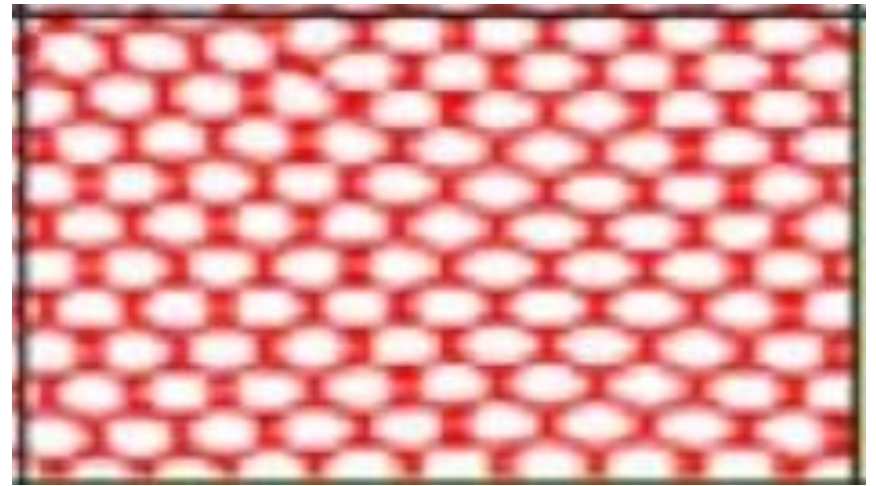
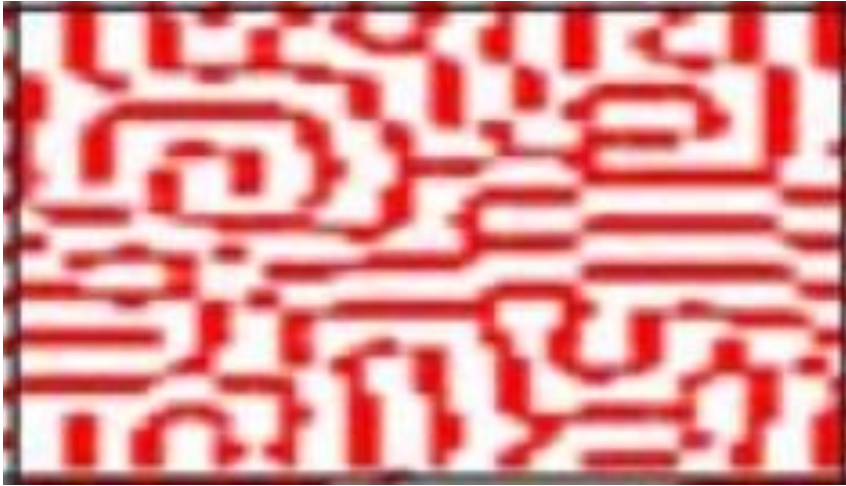
Behaviour-induced spatial morphology

$$\phi_{ij}^x(\mathbf{I}, \mathbf{C} | \alpha^x, \omega) = Z_{x,i}^{-1} \exp(\alpha^x b_j - \omega c_{ij})$$

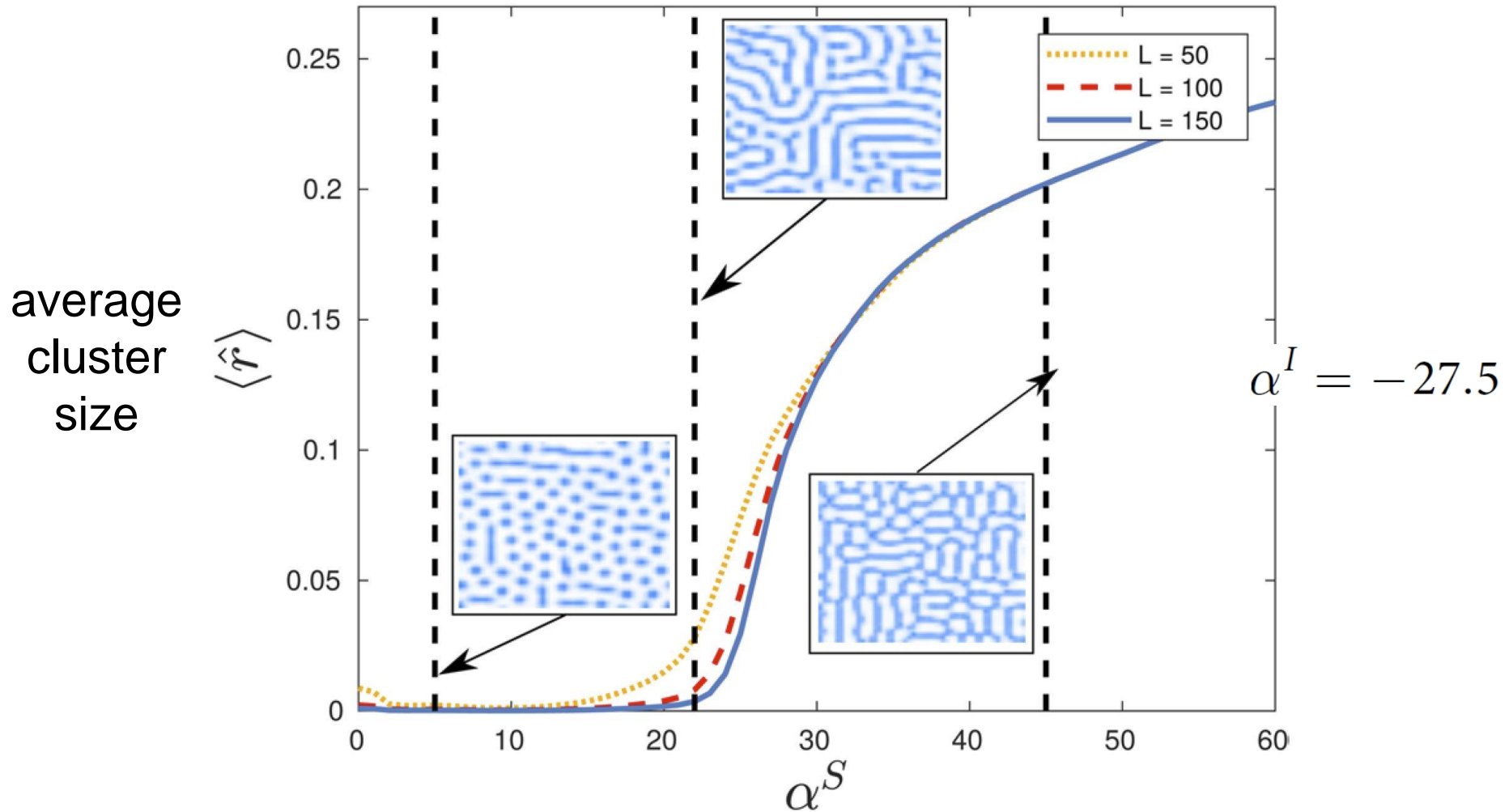




Patterns: spots, labyrinth, gaps, checkerboard



Spatial morphology: critical regimes



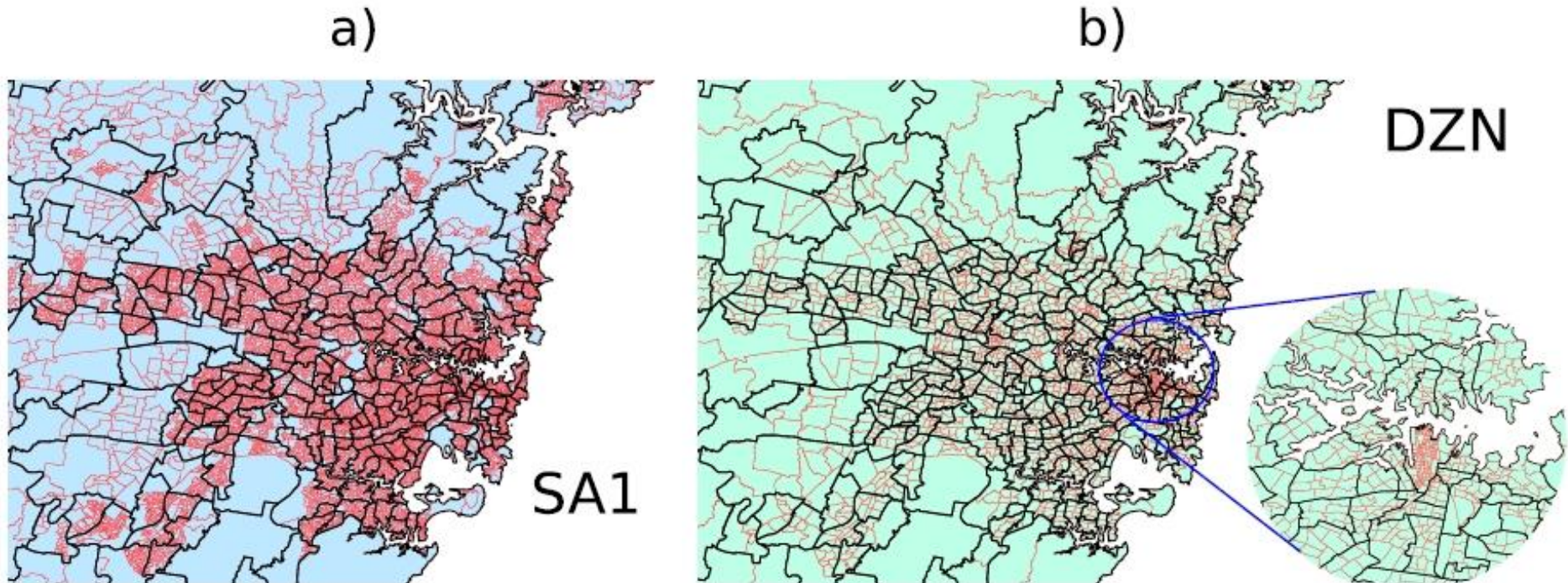
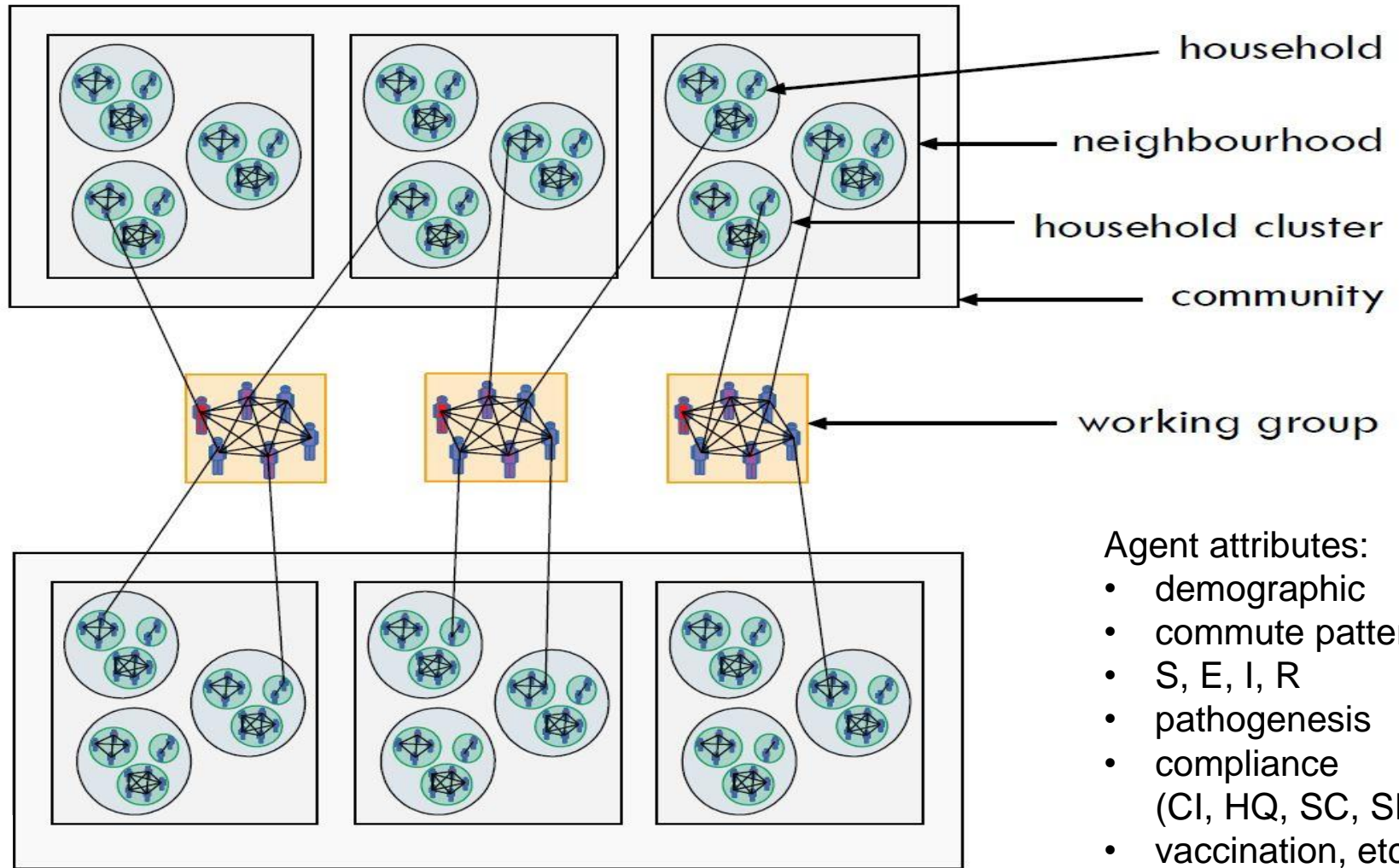


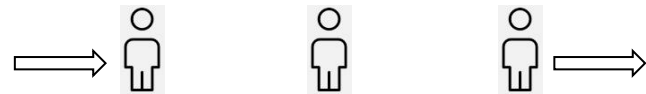
Fig. 1 Maps of the Greater Sydney region illustrating the distribution of population partitions. (a) A map of the Greater Sydney region showing SA2 (black) and SA1 (red) population partitions. (b) A map of the same area showing SA2 (black) and DZN (red) partitions. The inset in (b) zooms in on the Sydney central business district to illustrate the much denser packing of DZN partitions in that area.

“Same storm, different boats”



Features of our ABM (AMTraC-19)

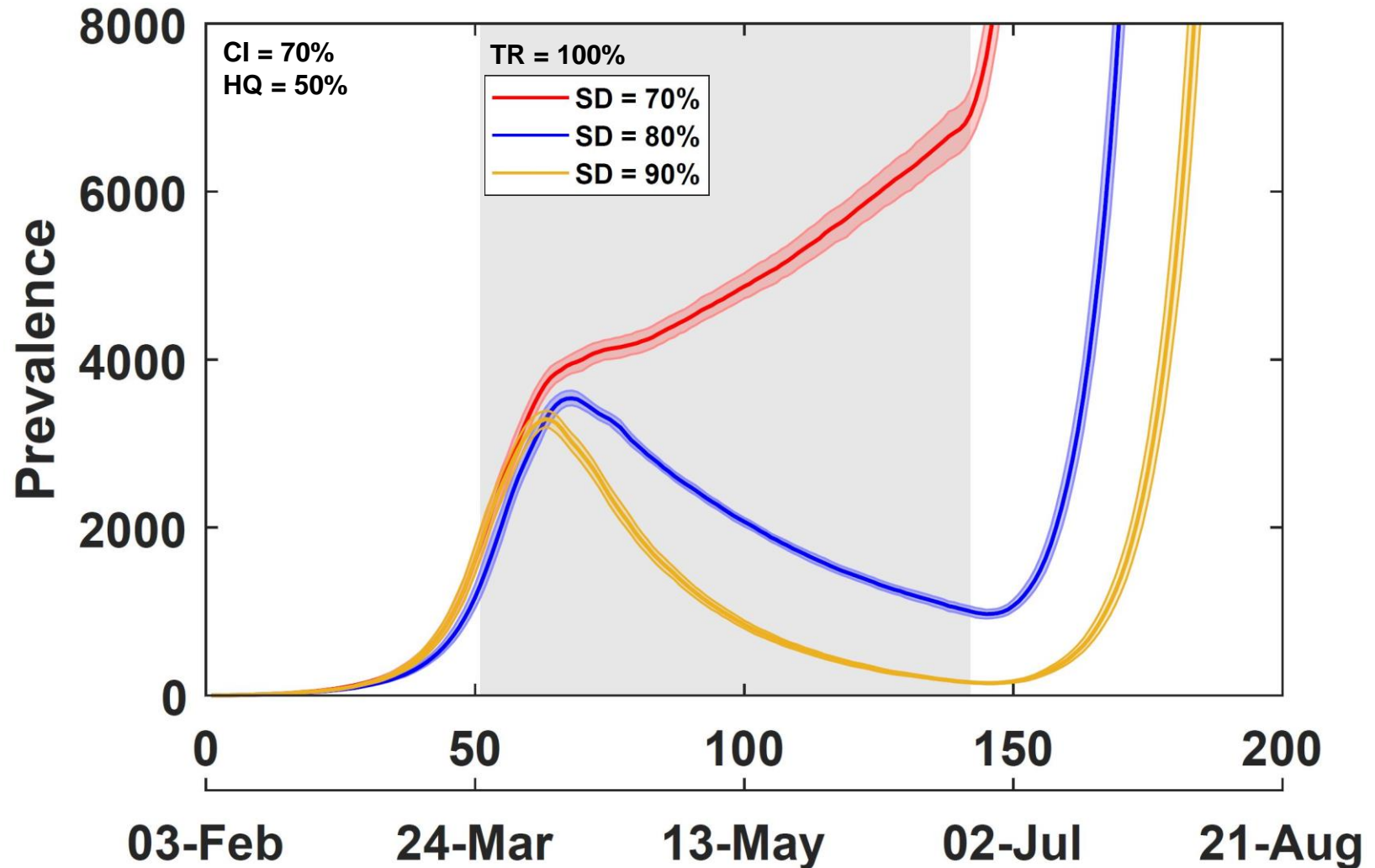
- ~24M stochastically generated agents (Census, ABS & ACARA data)
- household size and composition vary across different local areas
- commuting patterns between residence and work / study
- flexible infection seeding scenarios
- transmission within mixing contexts
- different symptomatic ratios for children and adults
- vaccination rollout with two vaccines
- vaccine efficacy split across components (infection, symptoms, transmission)
- varying compliance with lockdown (“stay-at-home” restrictions)



S. L. Chang, N. Harding, C. Zachreson, O. M. Cliff, M. Prokopenko, Modelling transmission and control of the COVID-19 pandemic in Australia, *Nature Communications*, 11, 5710, 2020.

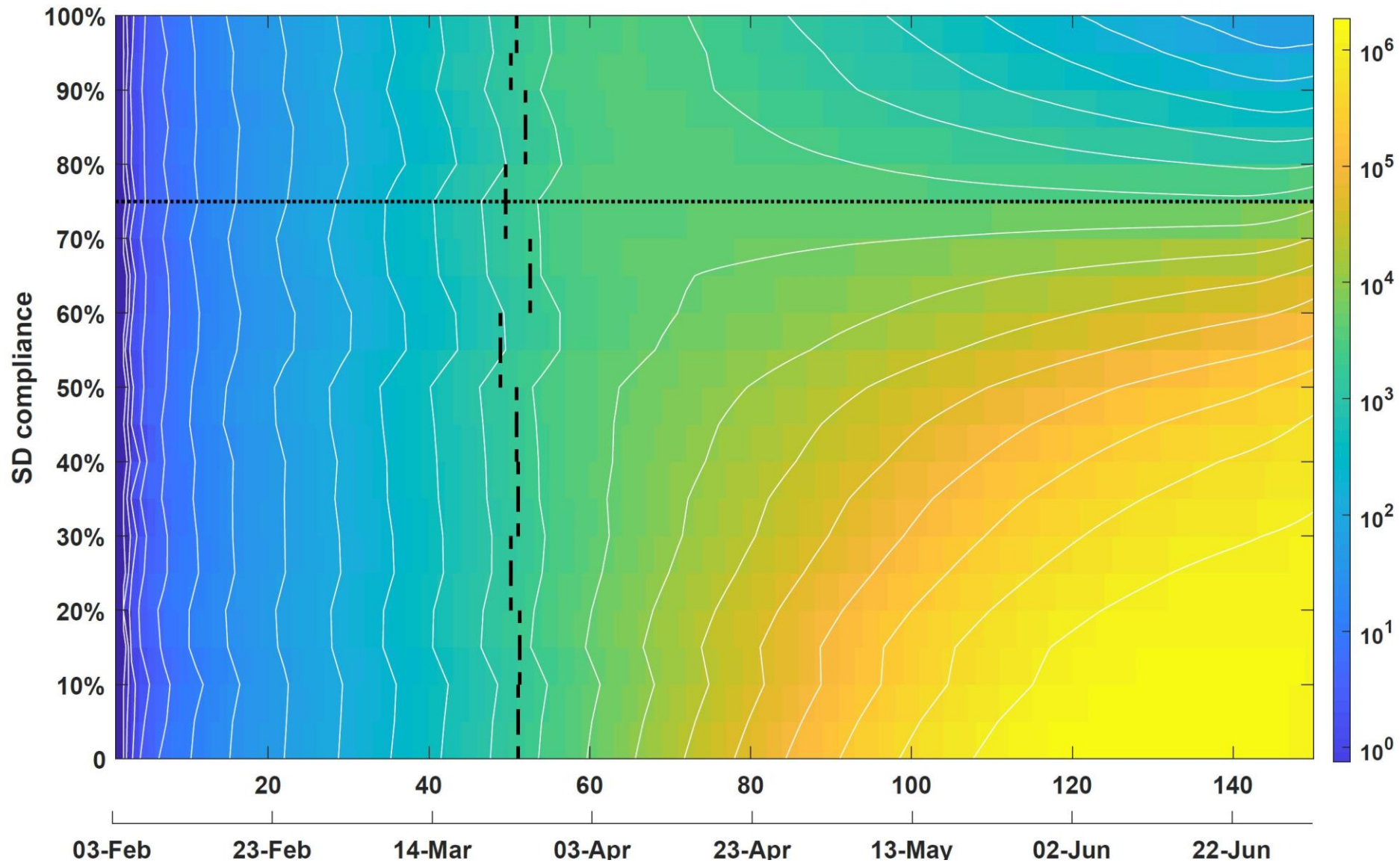
C. Zachreson, S. L. Chang, O. M. Cliff, M. Prokopenko, How will mass-vaccination change COVID-19 lockdown requirements in Australia? *The Lancet Regional Health – Western Pacific*, 14: 100224, 2021.

Tipping point in compliance with lockdown

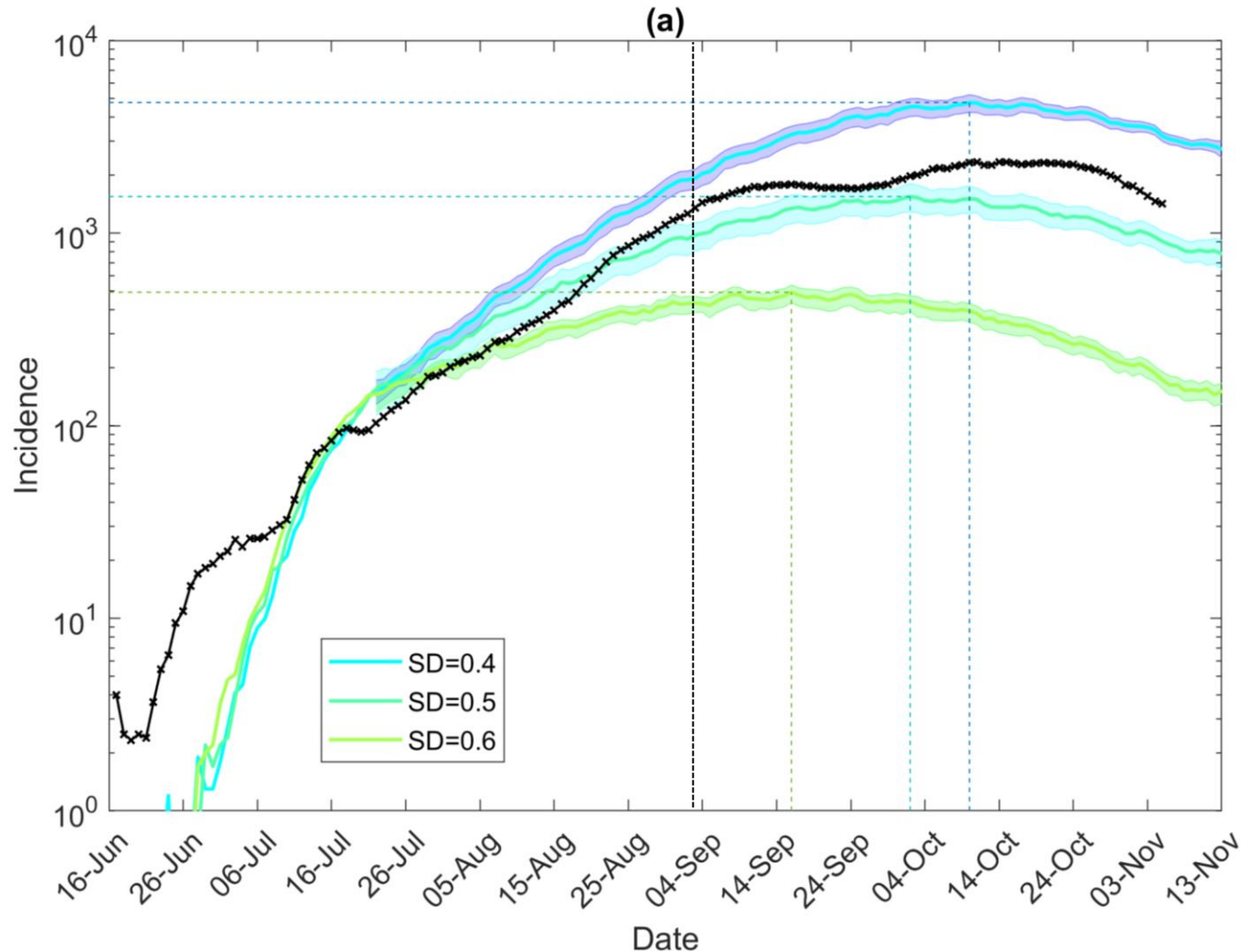




Tipping point (phase transition) in compliance

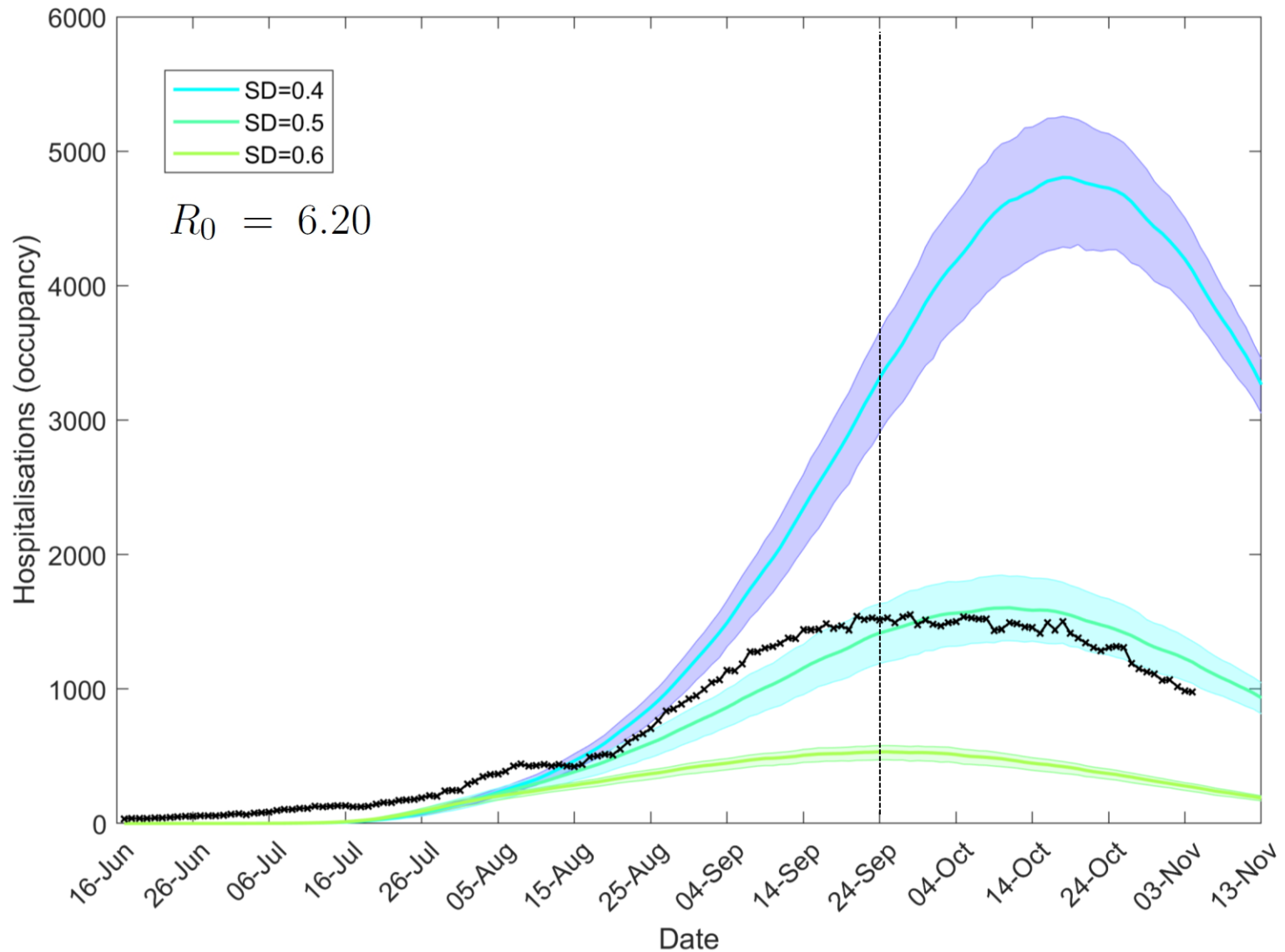


The Delta variant: SD compliance scenarios (25 August → 5 November 2021)



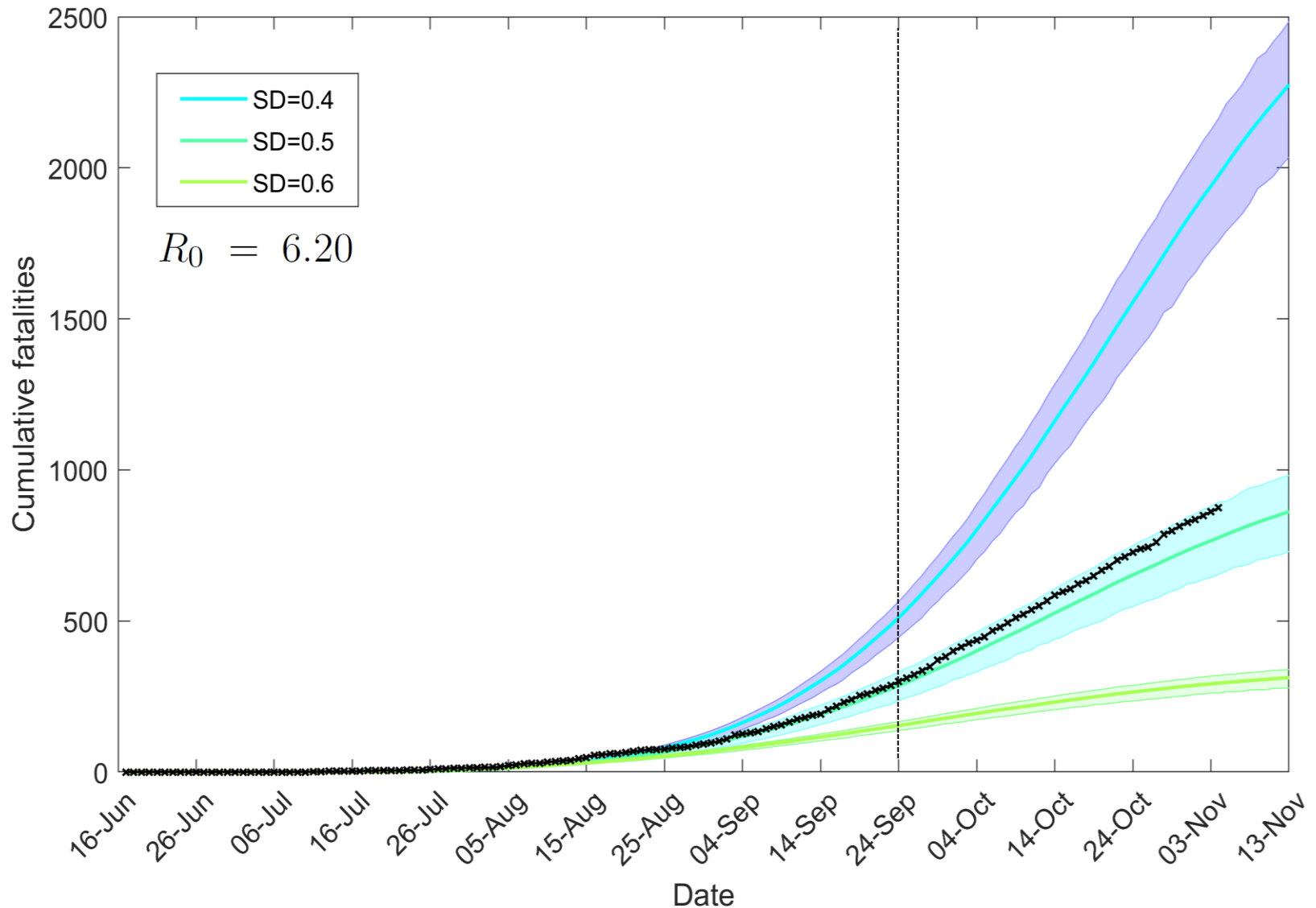
$$R_0 = 6.20$$

Hospitalisations (occupancy): a threefold reduction for 10% increase in compliance





Mortality (cumulative deaths): a two-fold reduction for 10% increase in compliance



- transitions in morphology (spots → labyrinth → gaps):
bounded rationality
- tipping points in pandemic response:
compliance with lockdown orders
- amplification effects of NPIs on disease burden:
compliance with lockdown orders

- N. Harding, R. E. Spinney, M. Prokopenko, Population mobility induced phase separation in SIS epidemic and social dynamics, *Scientific Reports*, 10: 7646, 2020.
- M. Prokopenko, J. T. Lizier, O. Obst, X. R. Wang, Relating Fisher information to order parameters, *Physical Review E*, 84, 041116, 2011.
- K. M. Fair, C. Zachreson, M. Prokopenko, Creating a surrogate commuter network from Australian Bureau of Statistics census data, *Scientific Data*, 6: 150, 2019.
- C. Zachreson, K. M. Fair, N. Harding, M. Prokopenko, Interfering with influenza: nonlinear coupling of reactive and static mitigation strategies, *Journal of Royal Society Interface*, 17(165): 20190728, 2020.
- S. L. Chang, N. Harding, C. Zachreson, O. M. Cliff, M. Prokopenko, Modelling transmission and control of the COVID-19 pandemic in Australia, *Nature Communications*, 11: 5710, 2020.
- C. Zachreson, S. L. Chang, O. M. Cliff, M. Prokopenko, How will mass-vaccination change COVID-19 lockdown requirements in Australia?, *The Lancet Regional Health – Western Pacific*, 14: 100224, 2021.
- S. L. Chang, O. M. Cliff, C. Zachreson, M. Prokopenko, Simulating Transmission Scenarios of the Delta Variant of SARS-CoV-2 in Australia, *Frontiers in Public Health*, 10, 10.3389/fpubh.2022.823043, 2022.